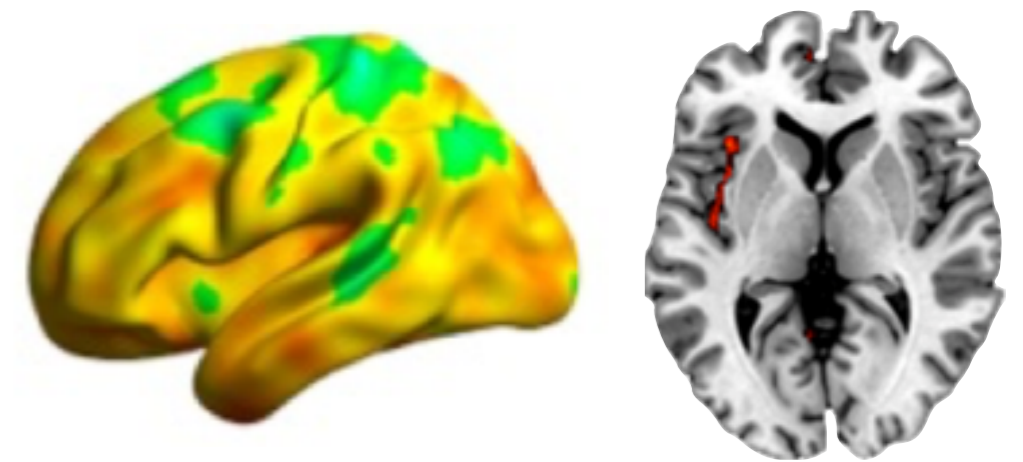


# 2-Sample T-test & Pair-T test [including some **tips** !?]



Kun-Hsien Chou, Ph.D (周坤賢)

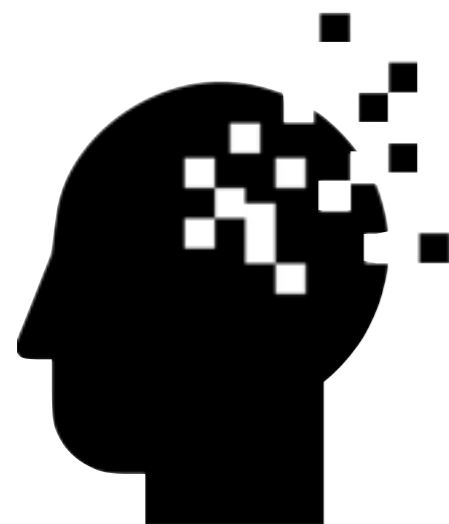
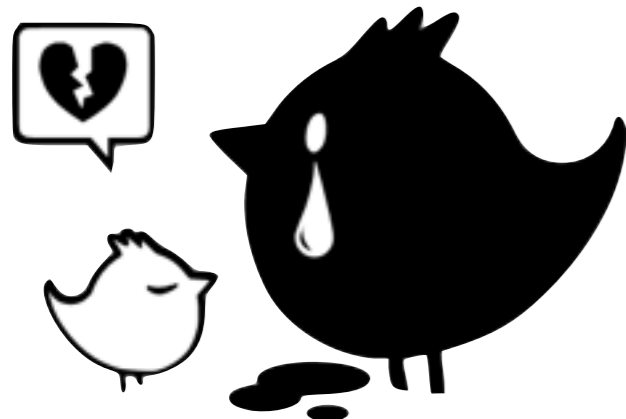
2017.07.19

Assistant professor | Institute of neuroscience | National Yang Ming University  
Assistant research fellow | Brain Research Center | National Yang Ming University



# In this **short** 90 mins course

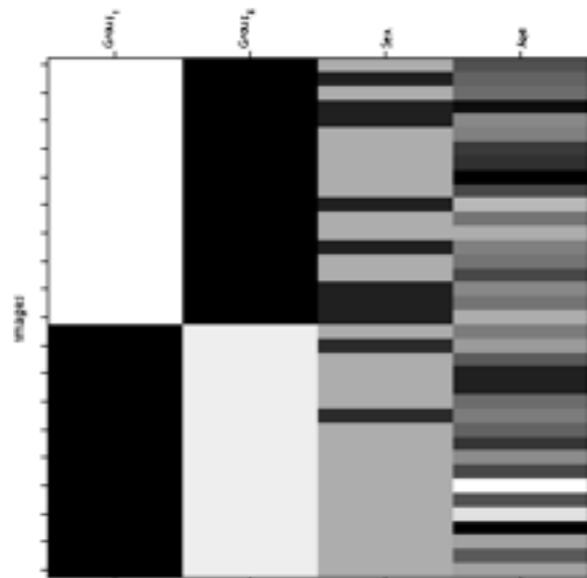
Real world  
**examples**



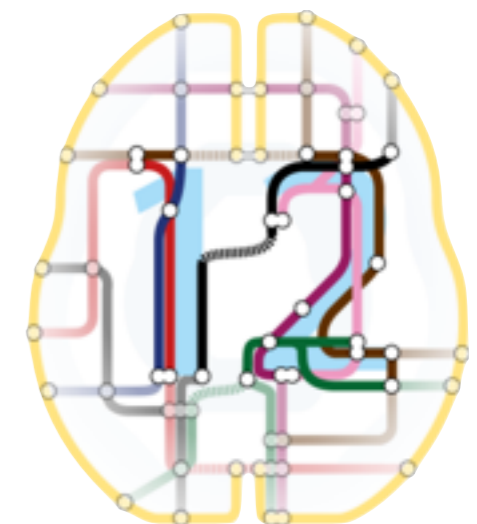
Mathematical  
formula

$$y = X\beta + \epsilon$$

The diagram illustrates the linear model equation  $y = X\beta + \epsilon$ . It shows a vertical vector  $y$  of size  $N$  (height) and width 1, a matrix  $X$  of size  $N$  (height) and  $p$  (width), a vertical vector  $\beta$  of size  $p$  (height) and width 1, and a vertical vector  $\epsilon$  of size  $N$  (height) and width 1.



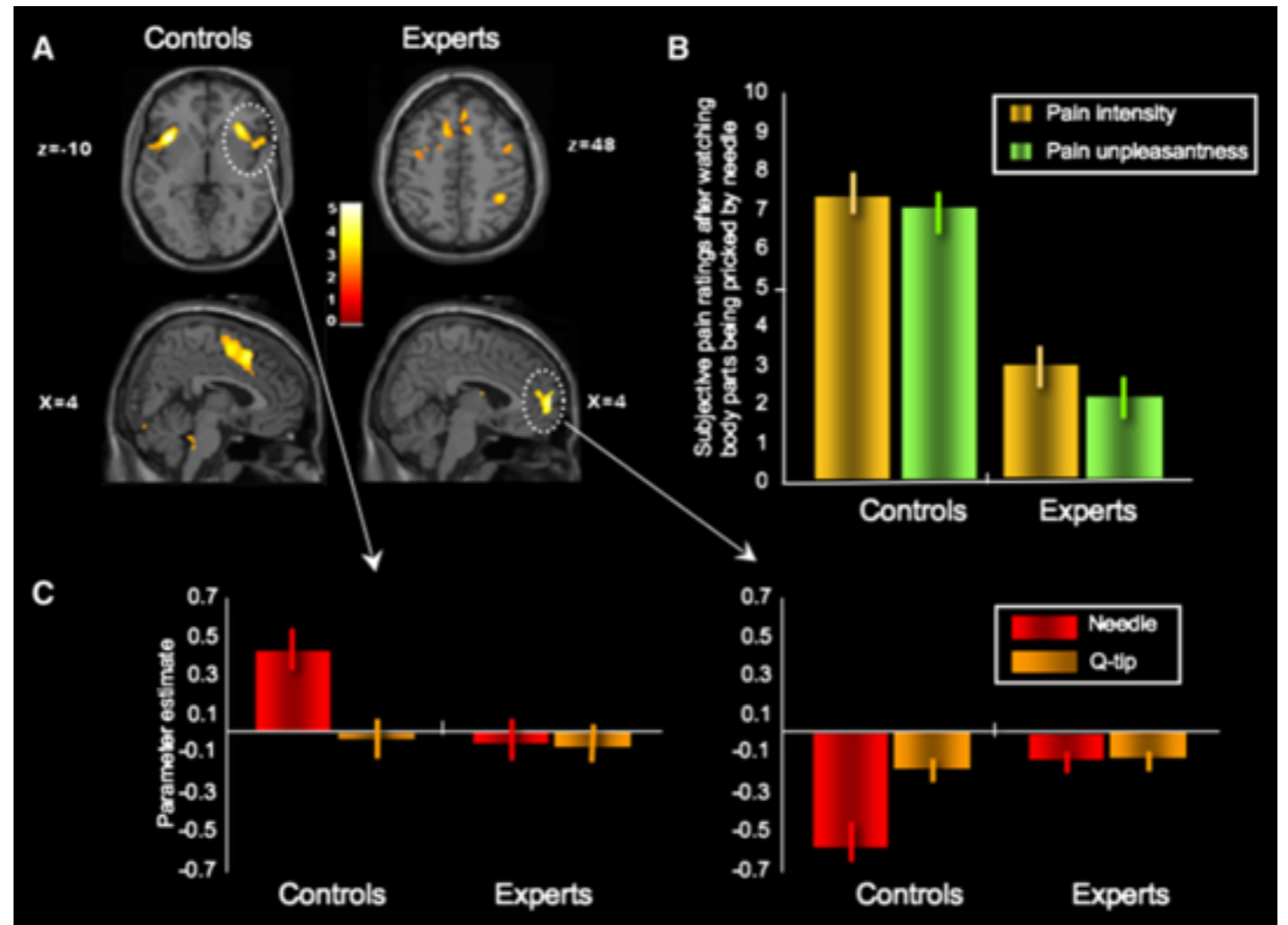
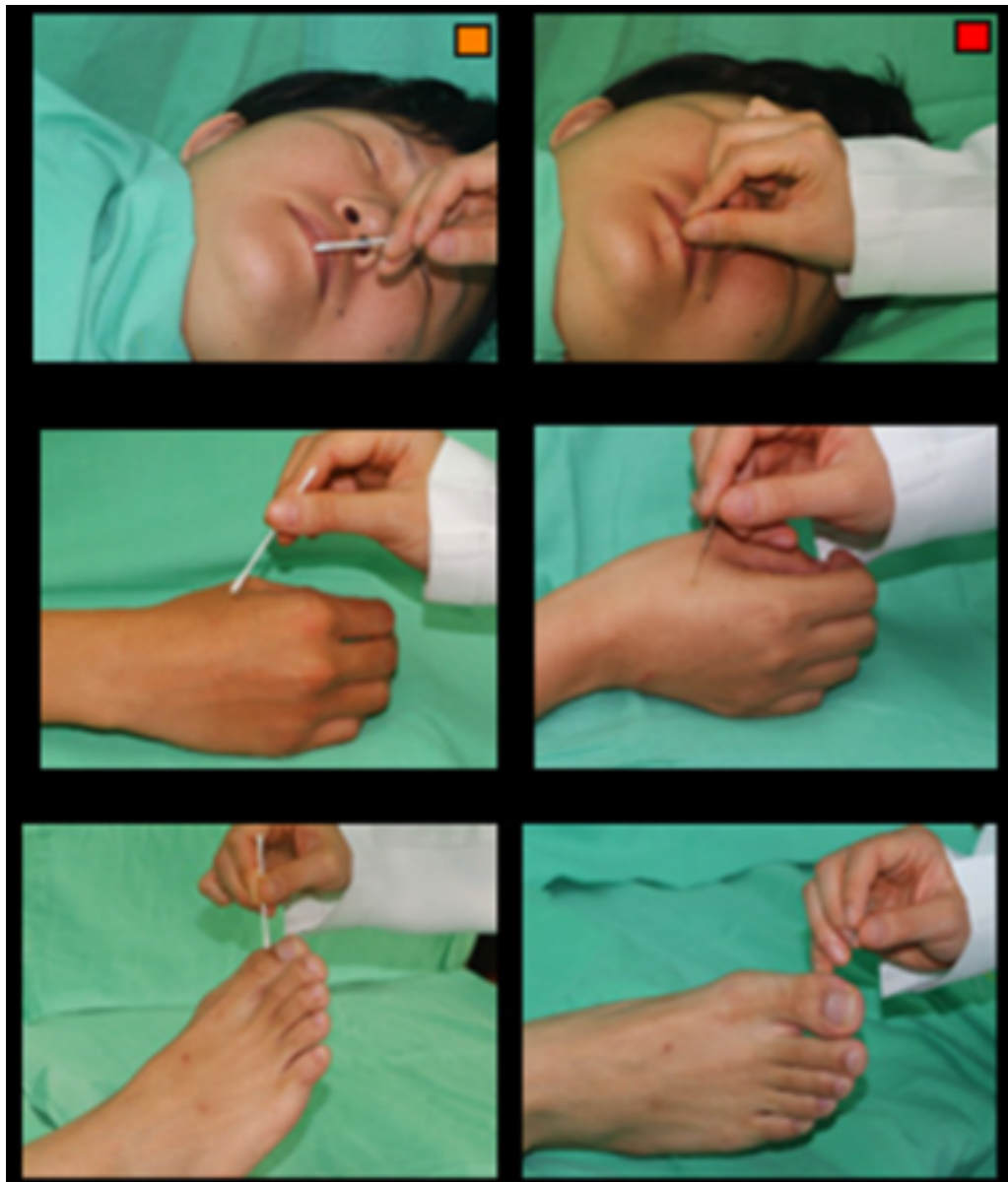
Answer with  
**SPM**



My first task-fMRI study. Almost ten years ago !

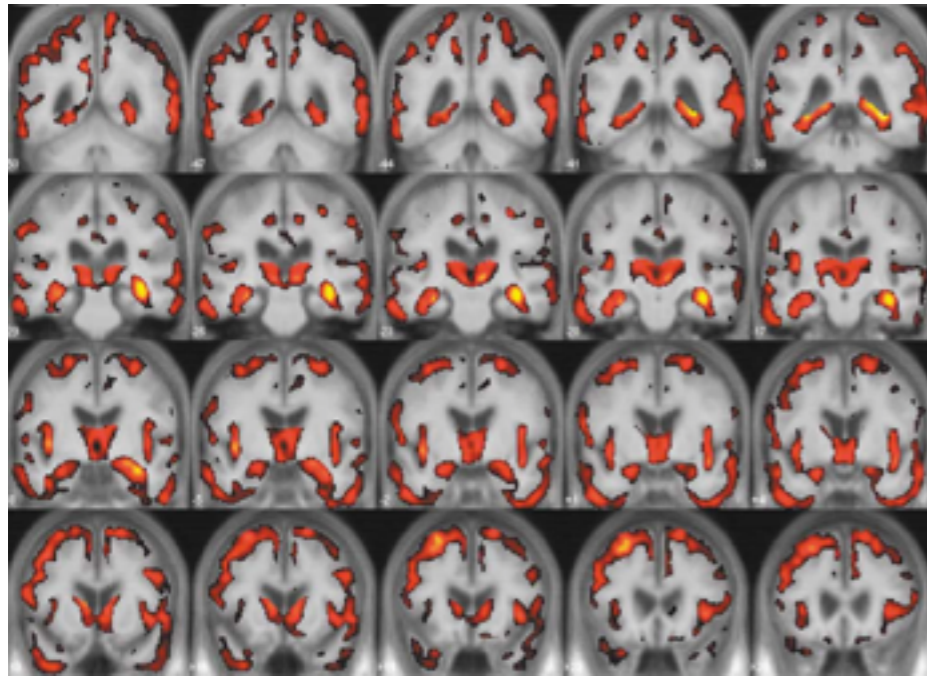


## Expertise Modulates the Perception of Pain in Others

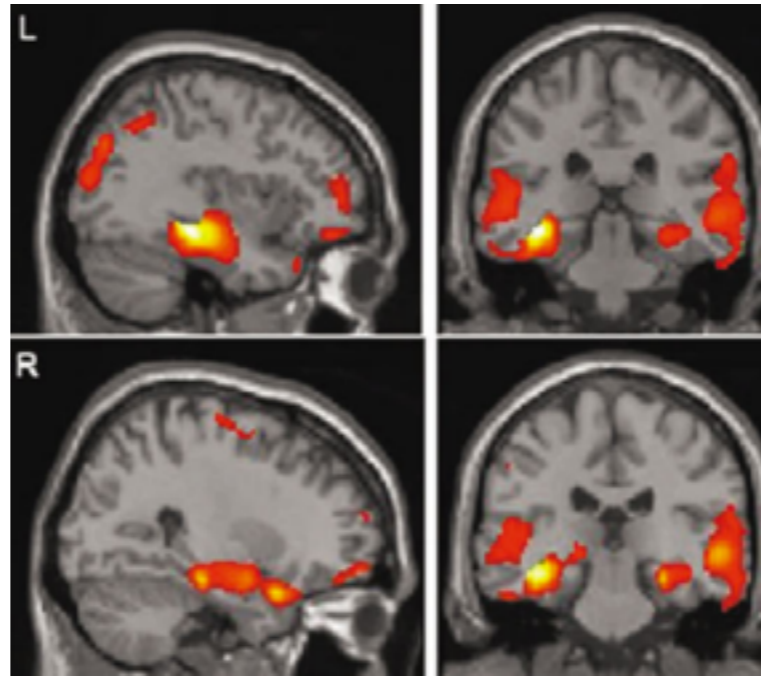


Experts using different stagey to perform their job !!

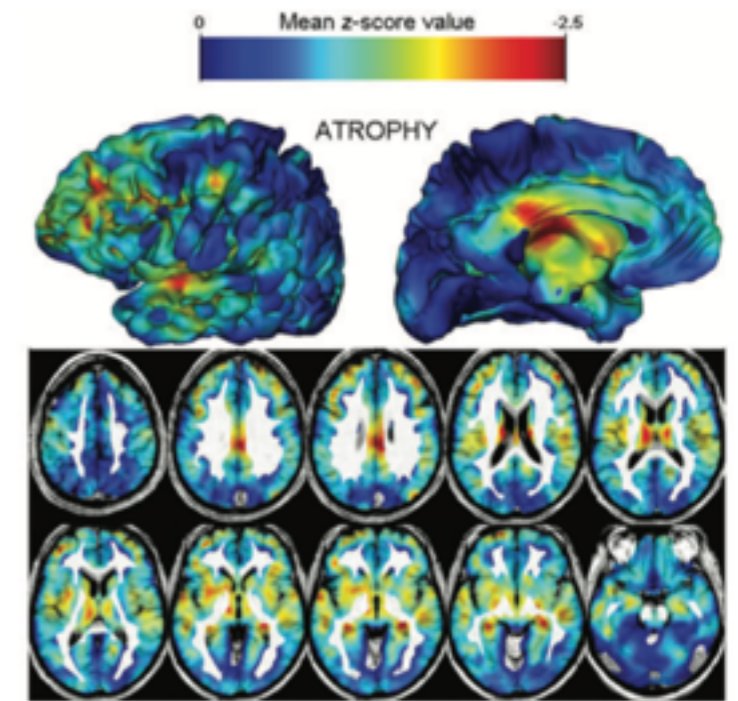
# Brain **morphometric** changes in patient with Alzheimer disease



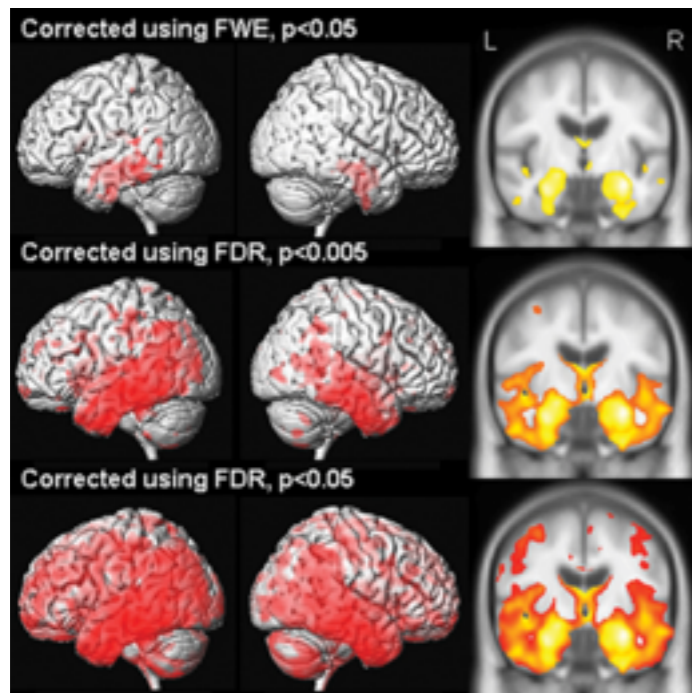
Karas et al. Neuroimage. 2003.



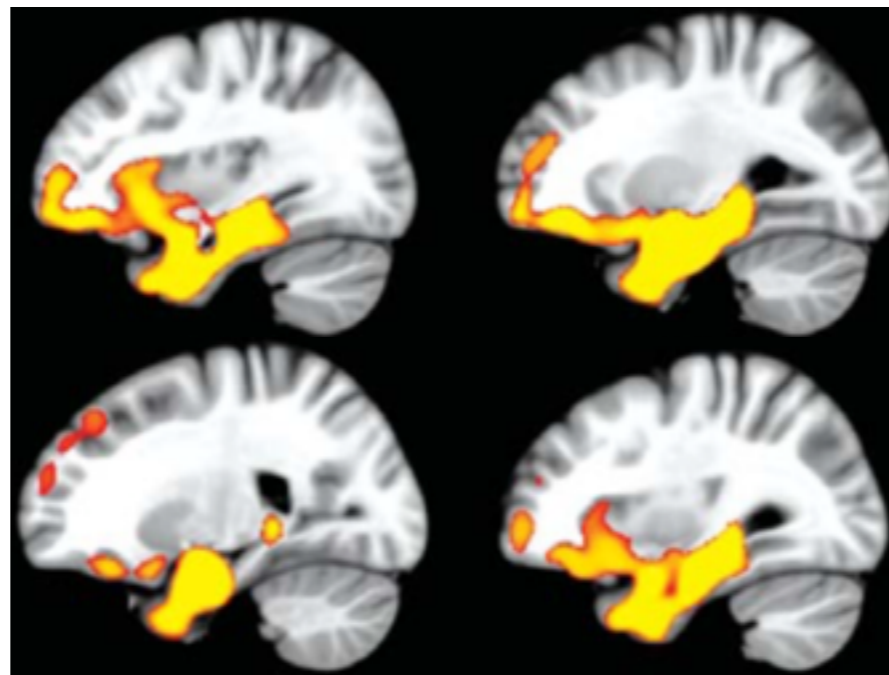
Testa et al. JMRI. 2004.



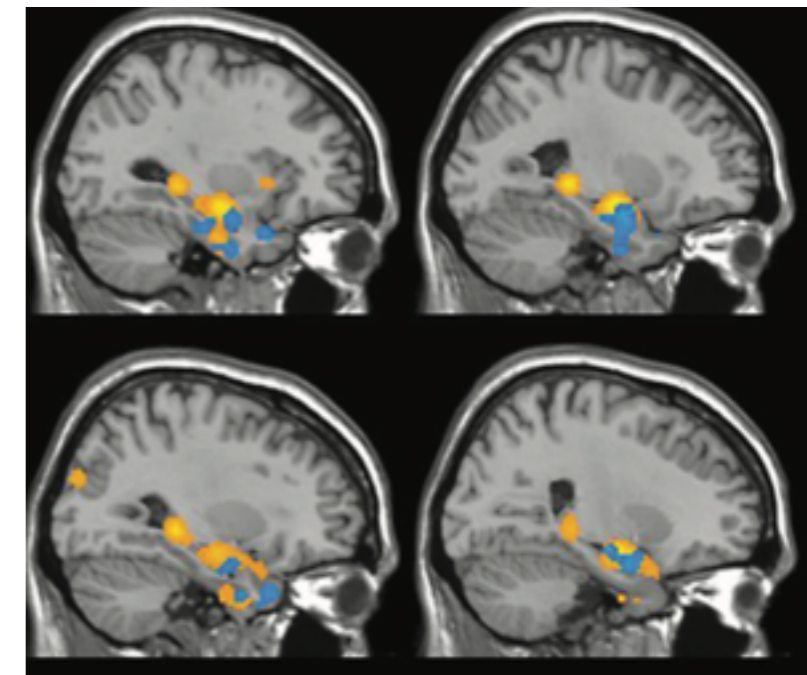
Chetelat et al. Brain. 2008.



Whitwell et al. Journal of neuroscience. 2009.

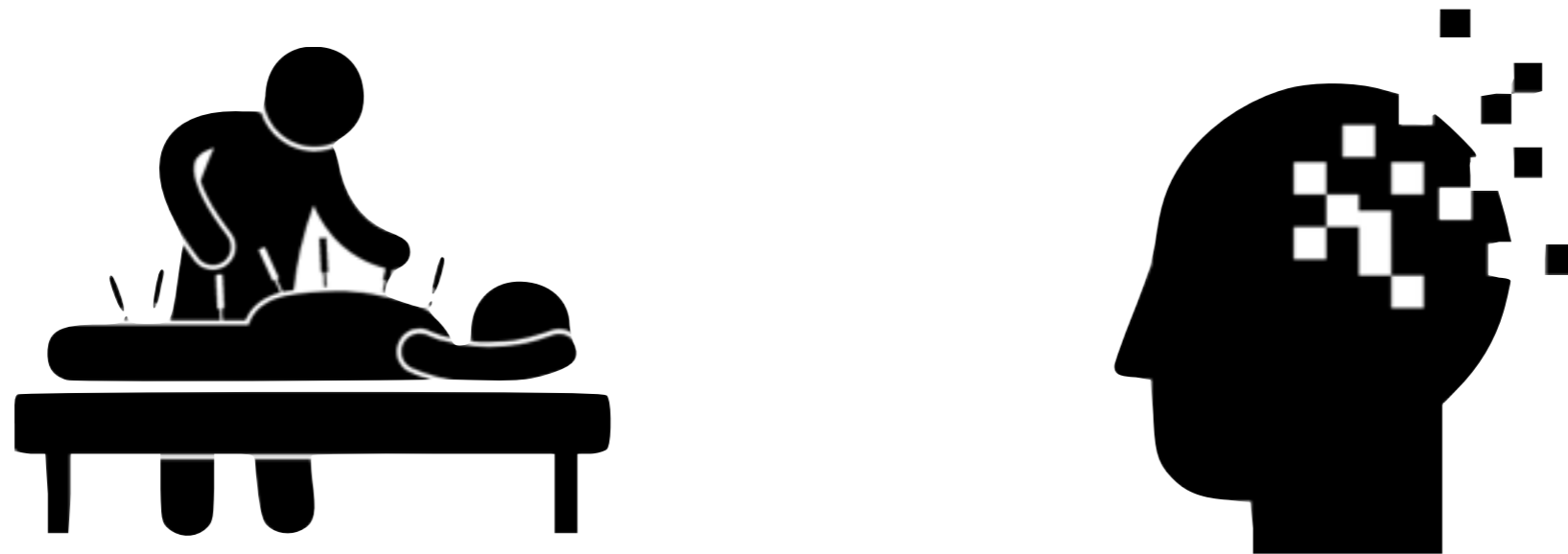


Wang et al. J. Alzheimers Dis. 2012.



Chapleau et al. J. Alzheimers Dis. 2016.

# Deconstructing the **framework** of scientific papers !



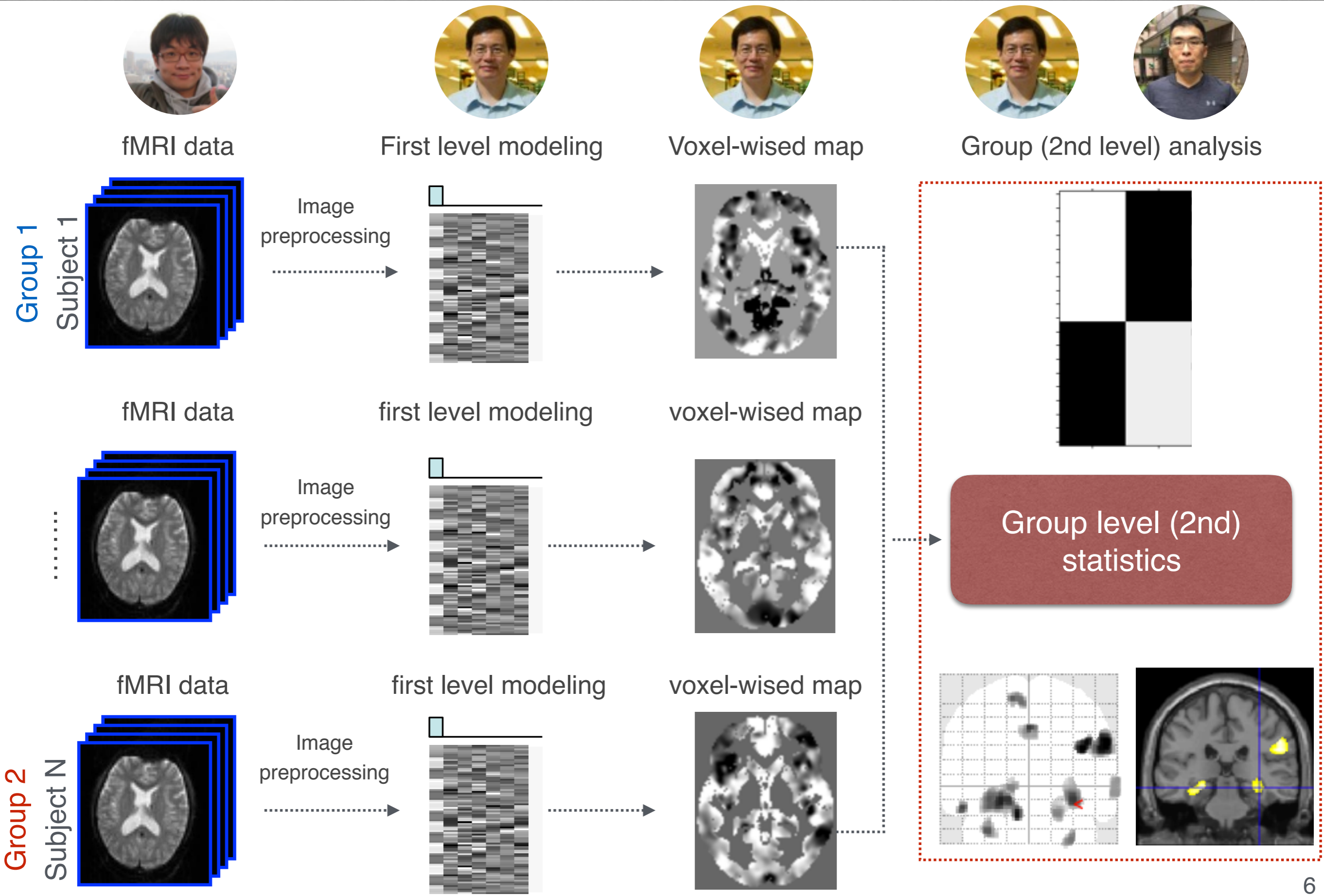
v.s.



control vs. experts  
healthy controls vs. AD

[2-sample T test]

# Recall your **memory** back !



# The **Interface** of Statistical Parametric Mapping

The screenshot displays the SPM12 software interface, divided into two main windows: 'Menu' and 'Graphics'.

**SPM12 (6685): Menu**

- Buttons: Real..., Norm..., Smooth, Core..., Segment.
- Section: Basic models (highlighted with a blue dashed border), Estimate (highlighted with a green dashed border), Results (highlighted with a red dashed border), Review, Bayesian, Dynamic Causal Modelling.
- Section: SPM for PET/SPECT
  - Buttons: Display, Check Reg, Re..., PET, To..., PPIs, ImCalc, DICOM Import, Help, Util..., Batch, Quit.

**SPM12 (6685): Graphics**

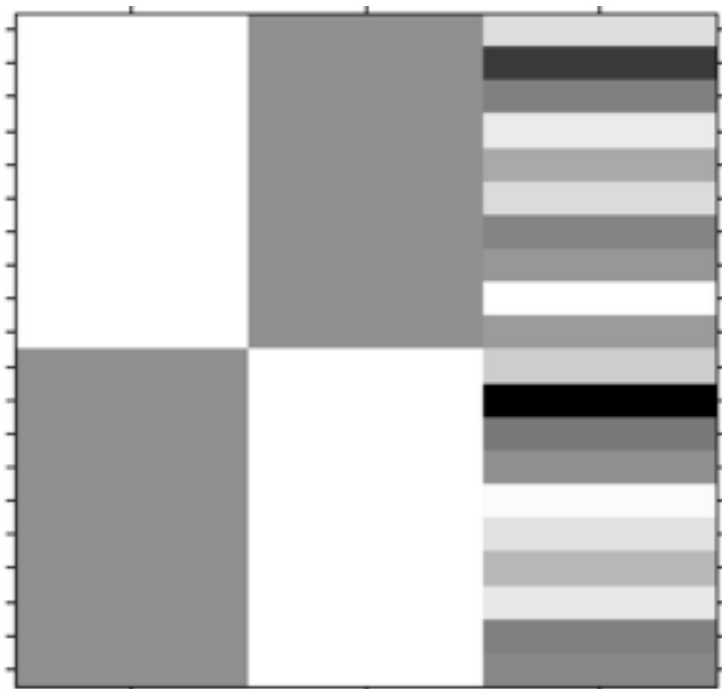
- Menu: File, Edit, View, Insert, Tools, Desktop, Window, SPM Figure, Help.
- Text: **Welcome to SPM12**  
Please refer to this version as "[SPM12](#)" in papers and communications.
- Diagram: A brain cross-section with a complex network of colored lines (yellow, blue, red, green, black, pink, brown) representing neural pathways or connections.
- Text: The SPM12 [Manual](#) and [Release Notes](#) are available as PDF documents in the *man* directory of your SPM installation.  
[Updates](#) will be made available from time to time and advertised on the [SPM mailing list](#). You can also check for updates by clicking [here](#).  
We would love to hear your comments or bug reports – please contact us at [<fil.spm@ucl.ac.uk>](mailto:fil.spm@ucl.ac.uk).  
SPM is developed under the auspices of the Functional Imaging Laboratory (FIL), the Wellcome Trust Centre for Neuroimaging (WTCN), in the Institute of Neurology at University College London (UCL), UK.  
SPM is free software; you can redistribute it and/or modify it under the terms of the [GNU General Public Licence](#) as published by the Free Software Foundation; either version 2 of the Licence, or (at your option) any later version.

Model Construction

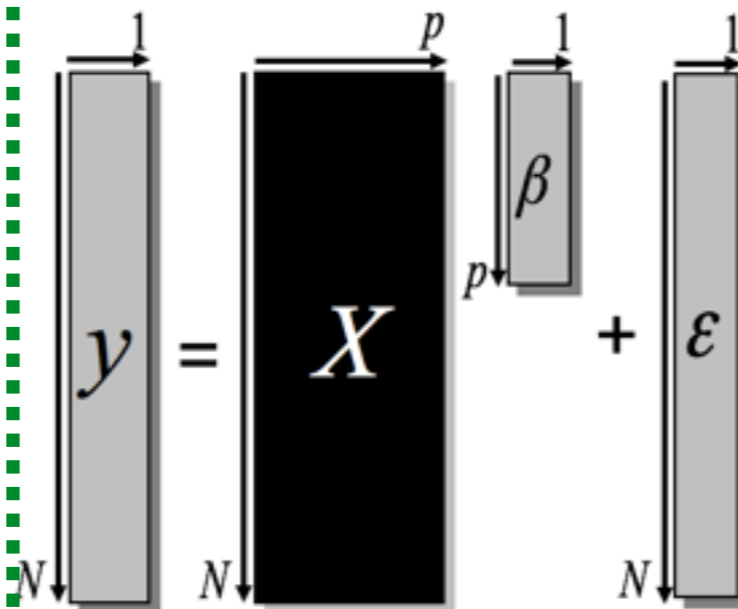
Model Estimation

Statistical Inference

# The basic statistical **pipeline** of SPM

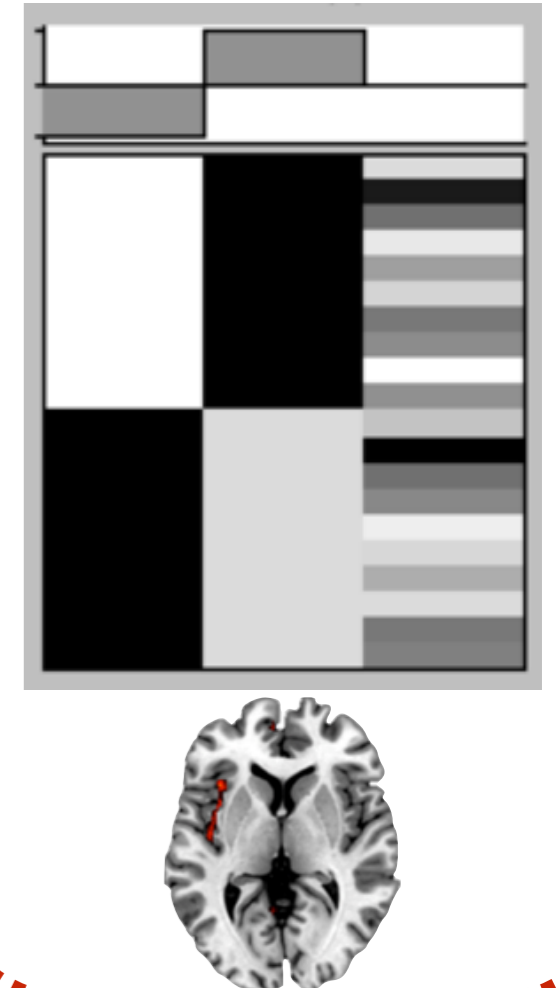


Model Construction



A diagram illustrating the model estimation step. It shows the linear model equation:  $y = X\beta + \epsilon$ . The vector  $y$  has a height of  $N$  and a width of 1. The matrix  $X$  has a height of  $N$  and a width of  $p$ . The vector  $\beta$  has a height of  $p$  and a width of 1. The vector  $\epsilon$  has a height of  $N$  and a width of 1.

Model Estimation



Statistical Inference



# General Linear Model - Modeling your scientific questions

**Why?** Make inferences about effects of interest

**How?**

- Decompose data into effects and error
- Form statistic using estimates of effects and error

$$Y = X^x \beta + E$$

Dependent Variable

(What you are measuring)

Independent Variable

(What you are manipulating)

Relative Contribution

(These need to be estimated)

Error

(The difference between the observed data and that which is predicted by the model)

Aim: To explain as much of the variance in Y by using X, and thus reducing E

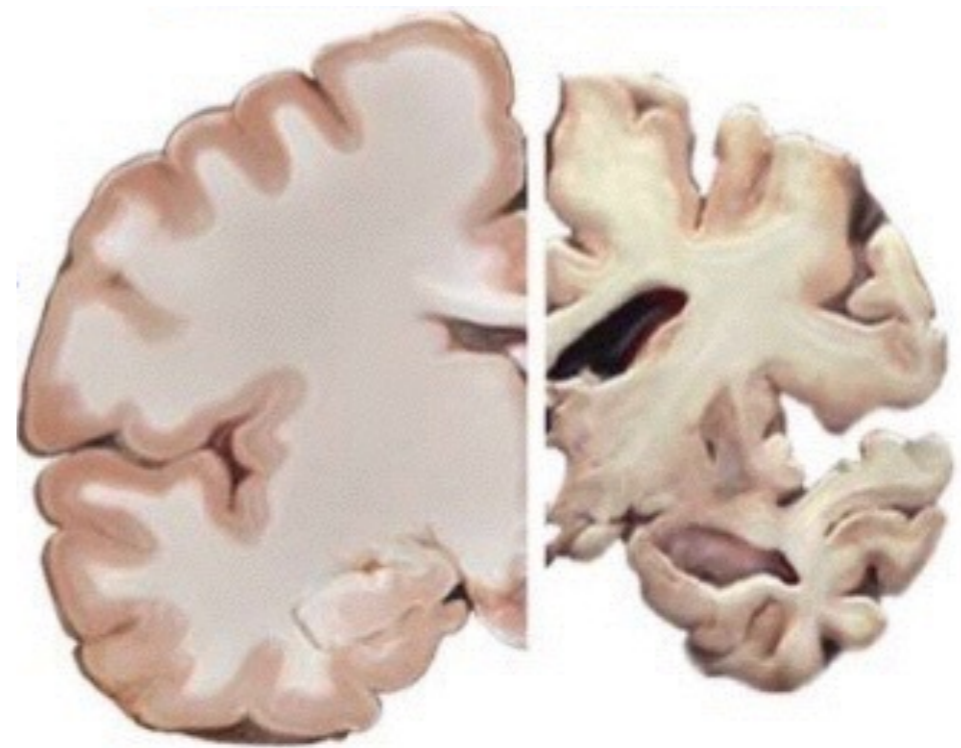
More than 1 EV ?  $Y = X_1\beta_1 + X_2\beta_2 + \dots X_n \beta_n \dots + E$

Univariate analysis !!

Example 1:

Is there any gray matter volume difference between healthy controls and patient with Alzheimer's disease !?

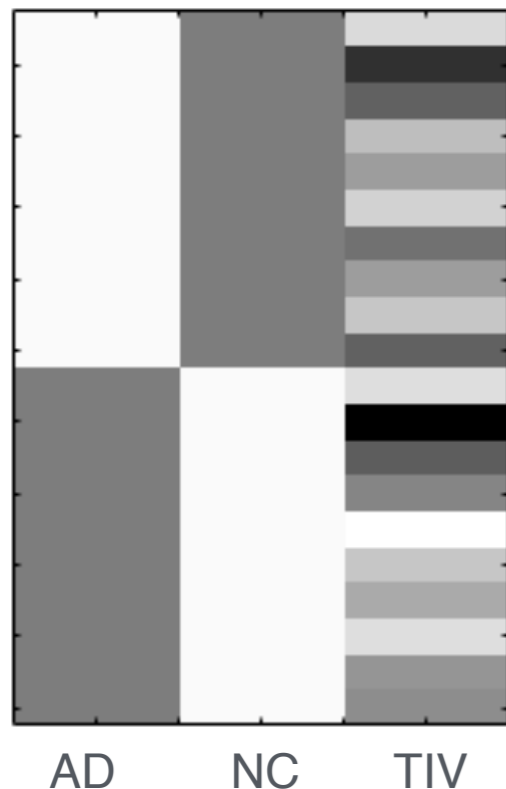
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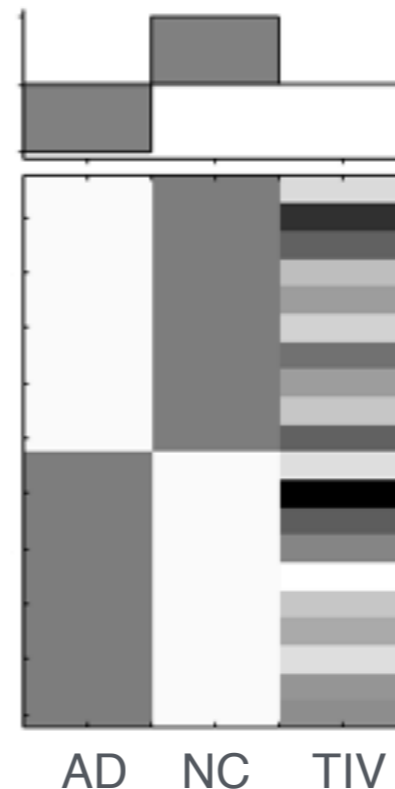
# Gray matter volume **atrophy** in patients with Alzheimer's disease

“Is there significantly **lower gray matter volume** in the patients with Alzheimer disease than in the healthy controls after adjusting total intracranial volume ?”

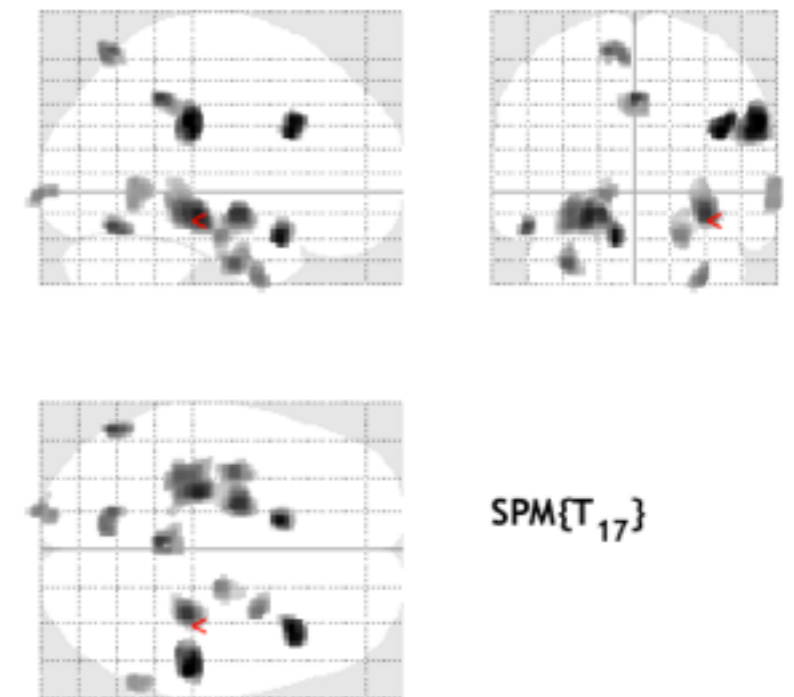
$$Y = \beta_1(\text{AD}) + \beta_2(\text{NC}) + \beta_3(\text{TIV}) + \varepsilon$$



Model construction

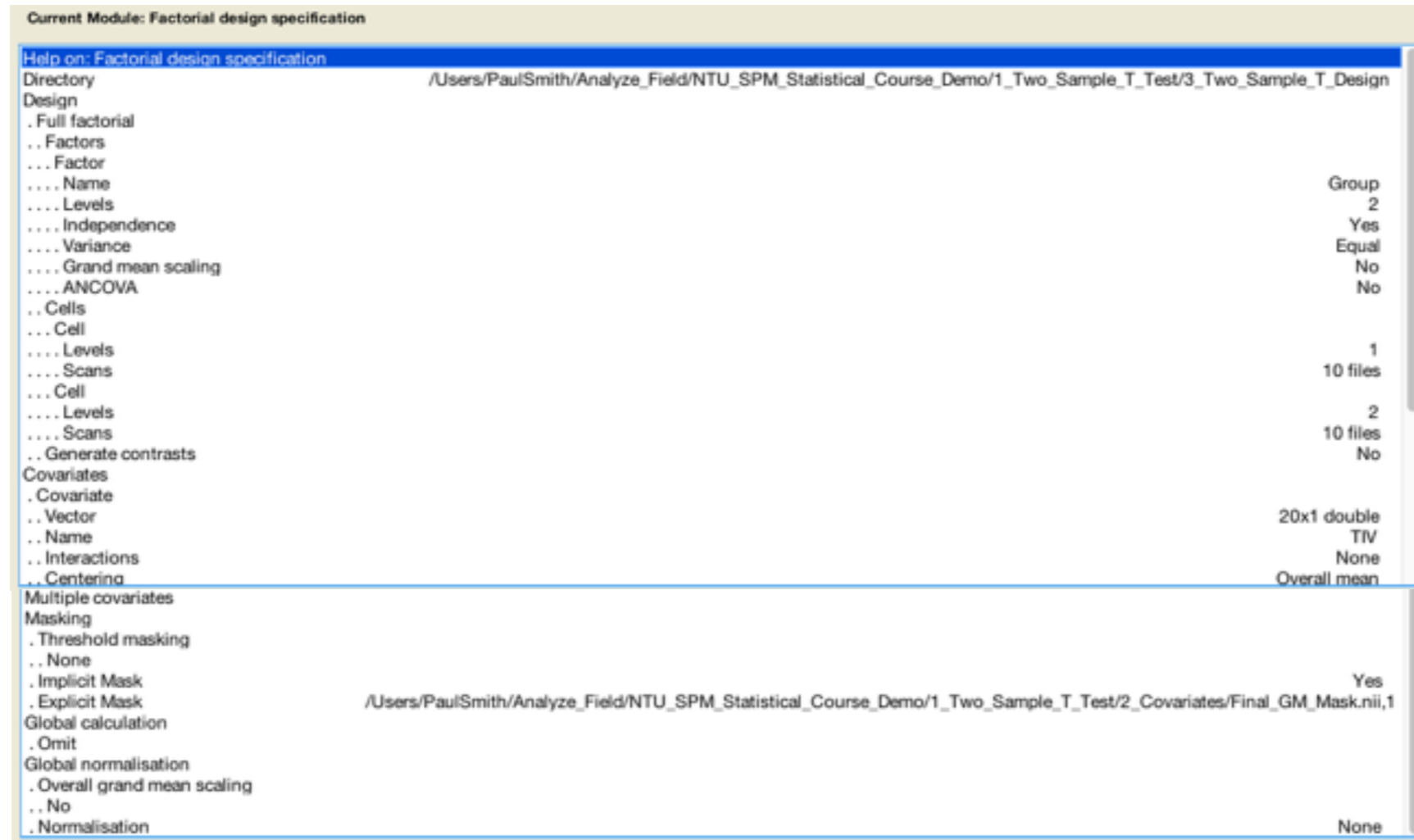


Statistical inference



Result visualization

# Full factorial design (Model Construction)



## Directory:

The output directory of your statistical model

## Design:

The statistical model you want to use (**Full factorial**)

[The definition of : Factors, Name, Level, Cell and Scans]

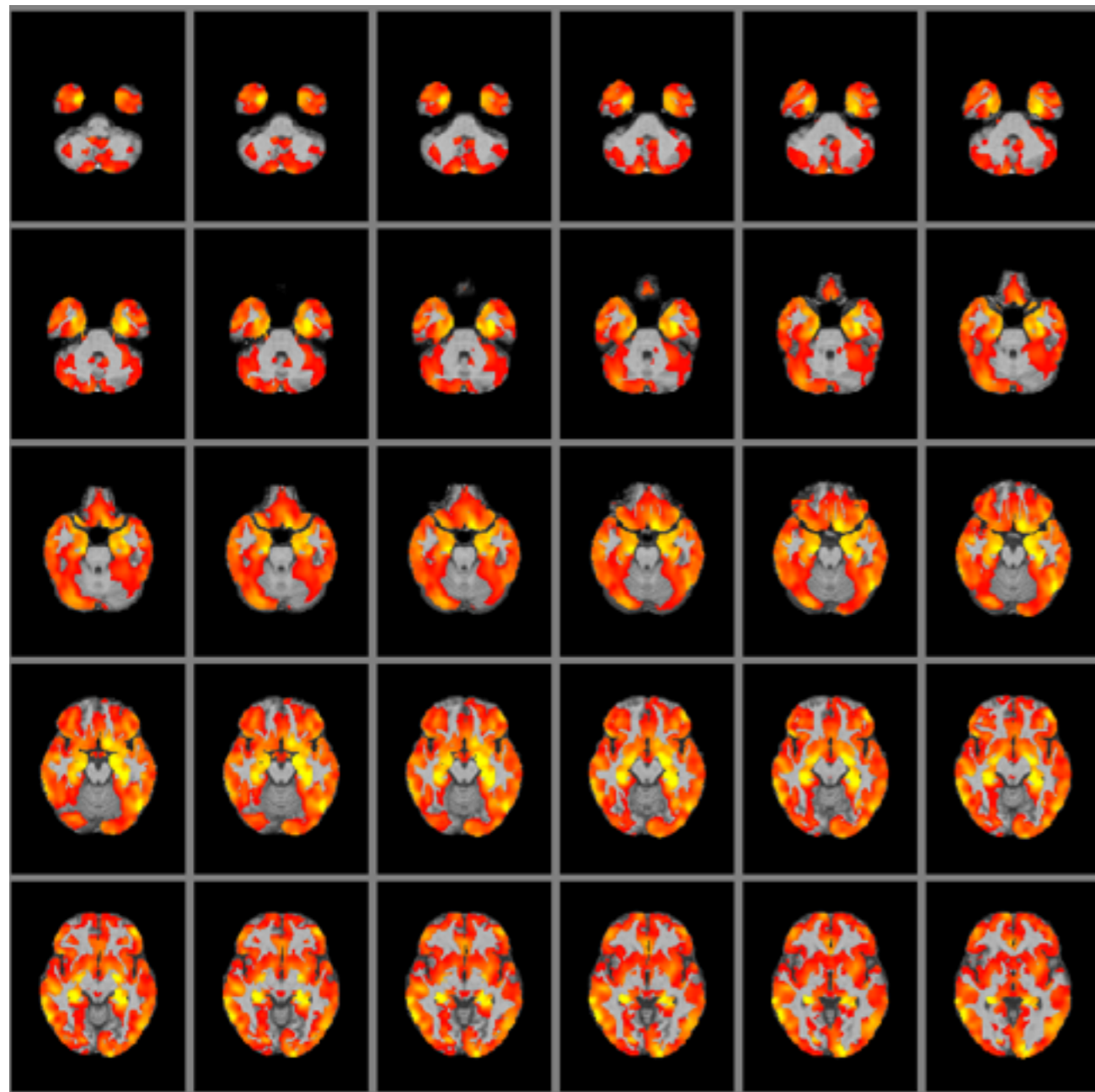
## Covariates:

The effect you want to adjust (TIV)

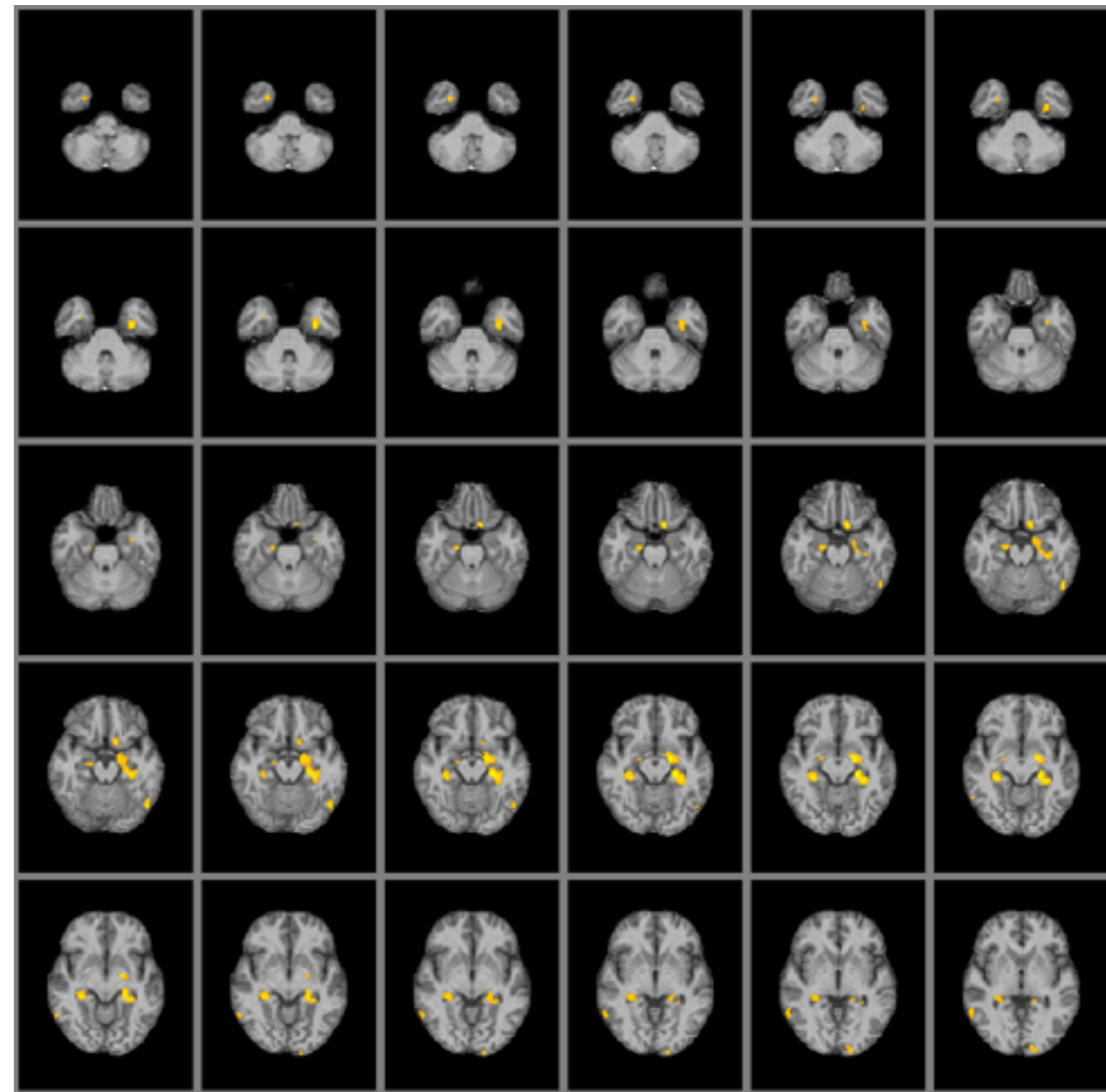
## Masking:

The region you want to do statistical inference (Absolute, implicit and explicit)

# Statistical **result** of our question !

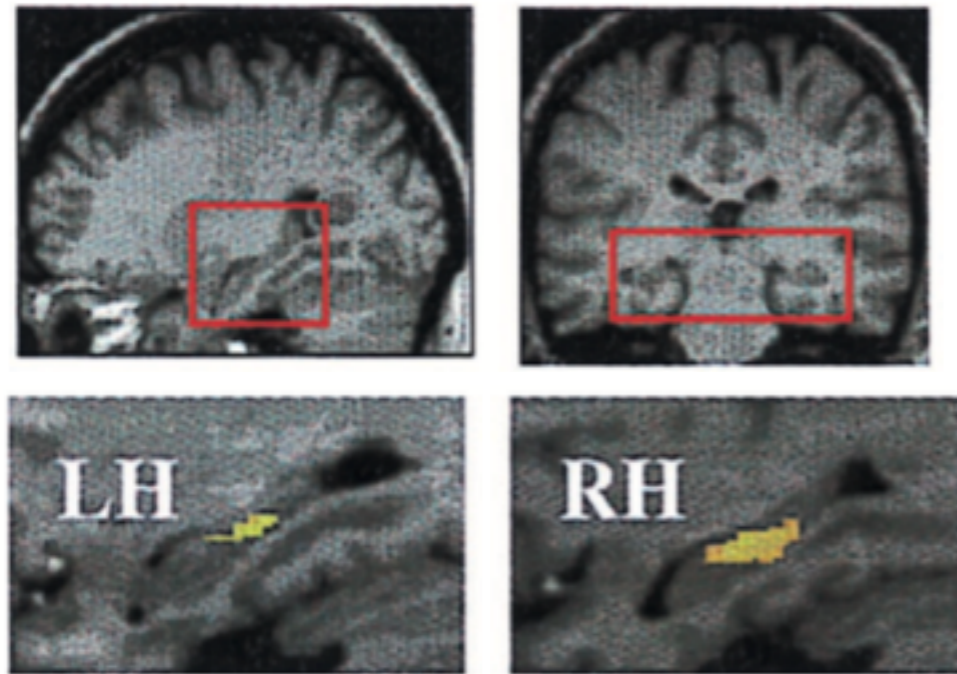


un-thresholded map

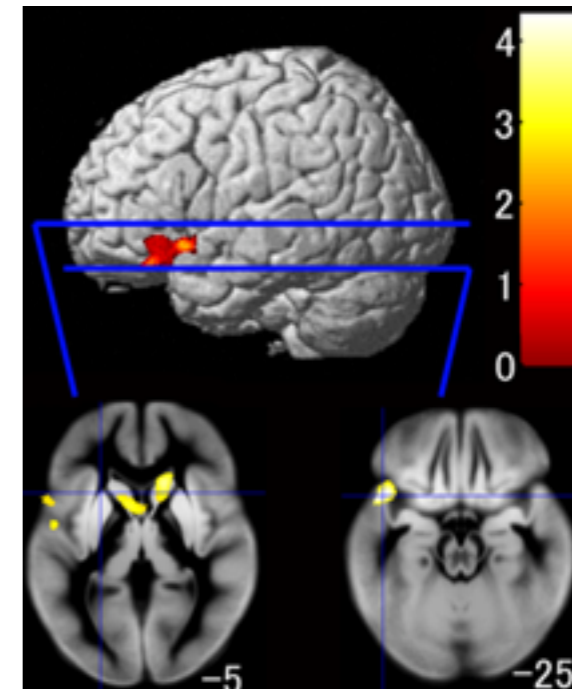


thresholded map

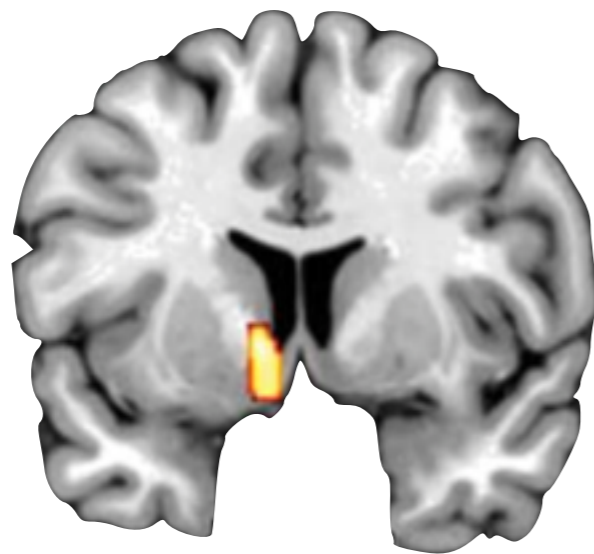
# Additional **real-world** examples using 2 sample T-test design



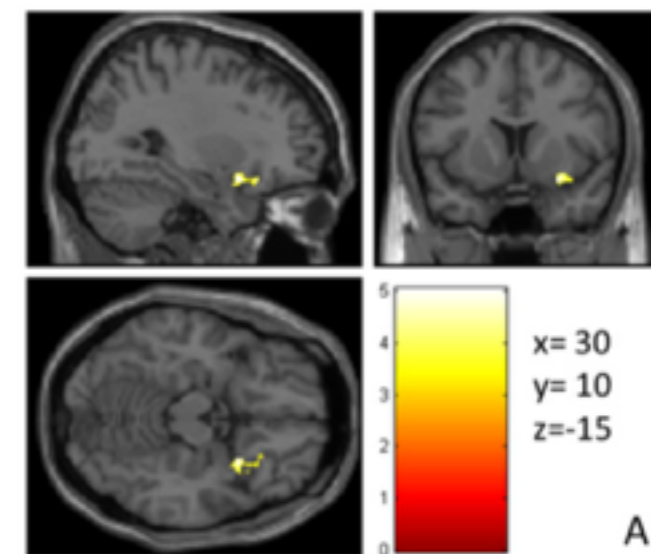
London taxi drivers vs. control subjects



rice for breakfast vs. bread for breakfast

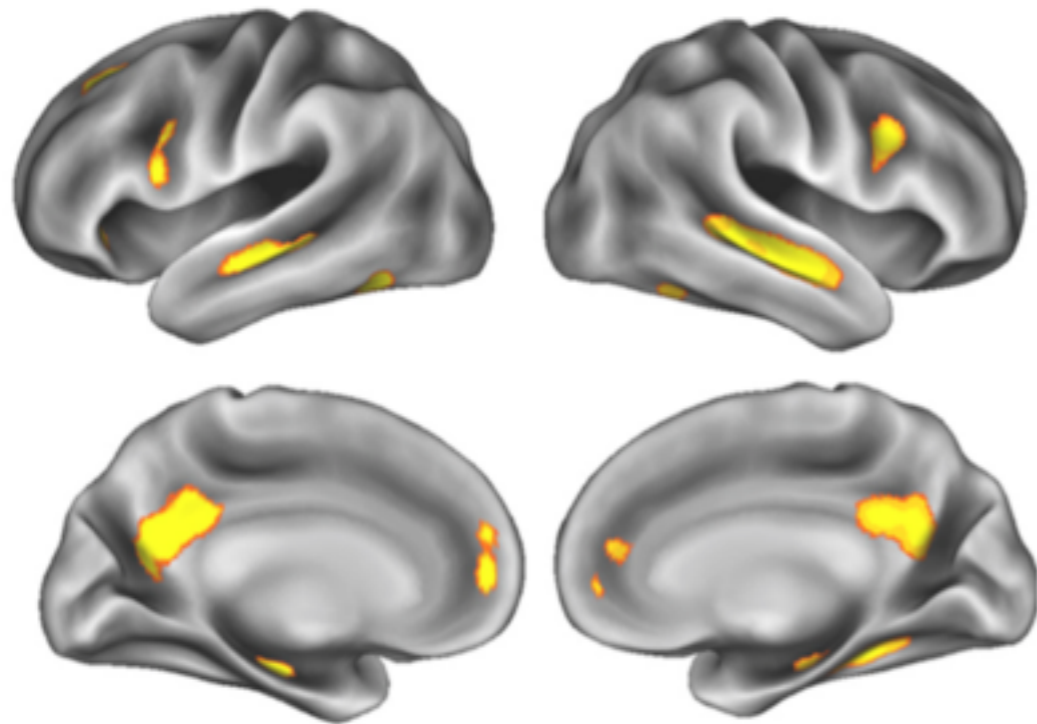


Frequent vs. infrequent video-gamers

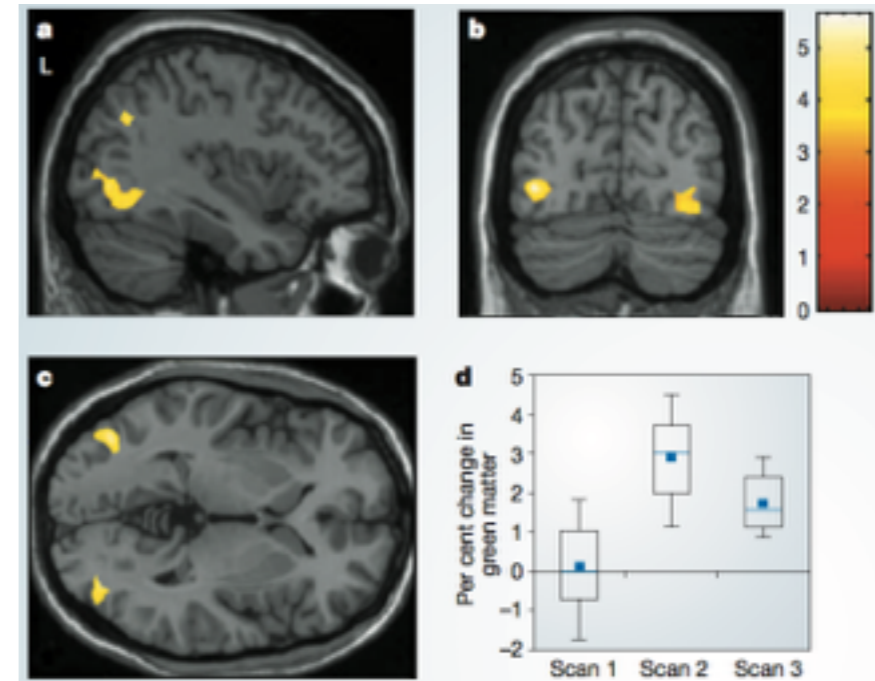


Yoga meditators vs. non-meditators

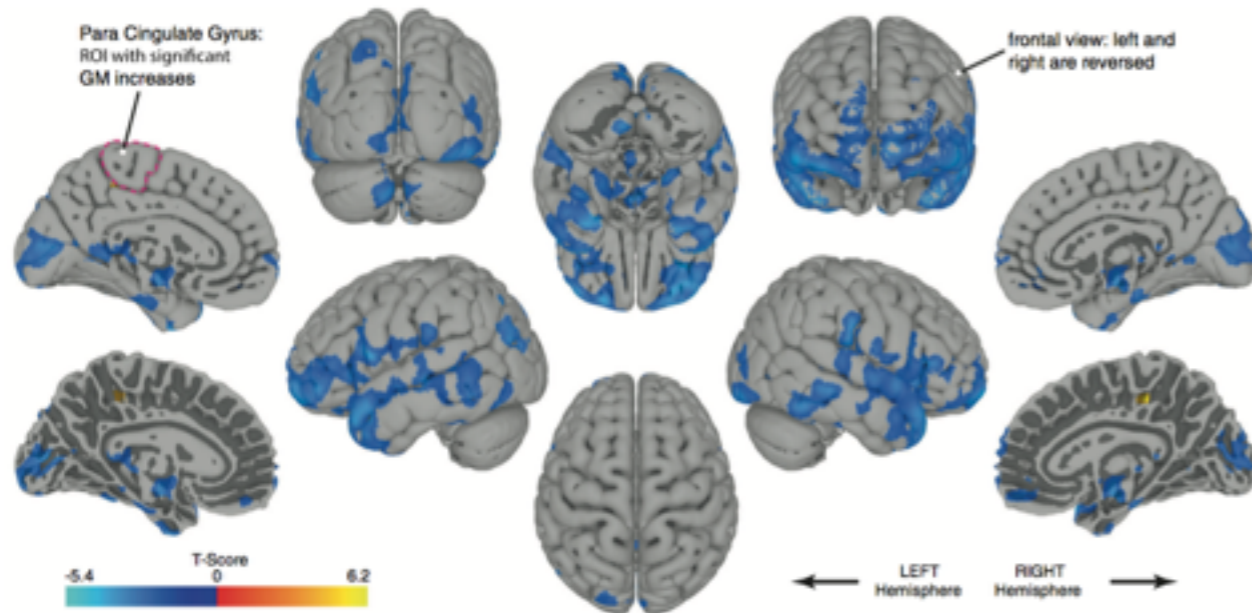
# We may also care about **before - after** effect .....



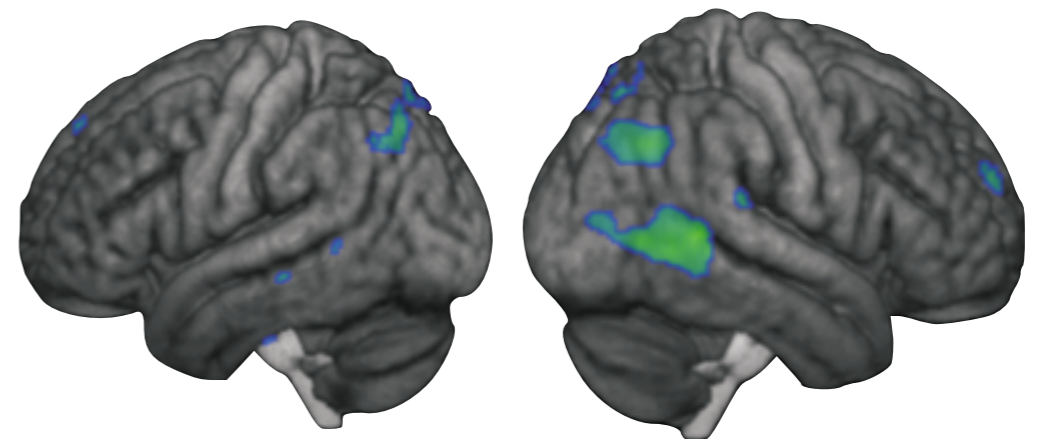
pre-pregnancy vs. post-pregnancy



Pre-training vs. post-training



pre-space flight vs. post-space flight



Before-ultra marathon vs. after 4001 km

# Or different experiment effects in **single** study group



Painful



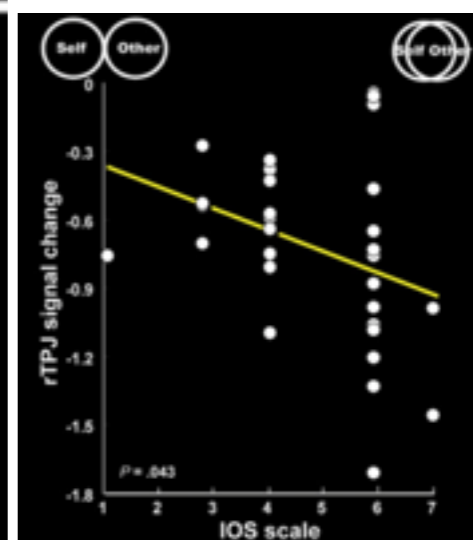
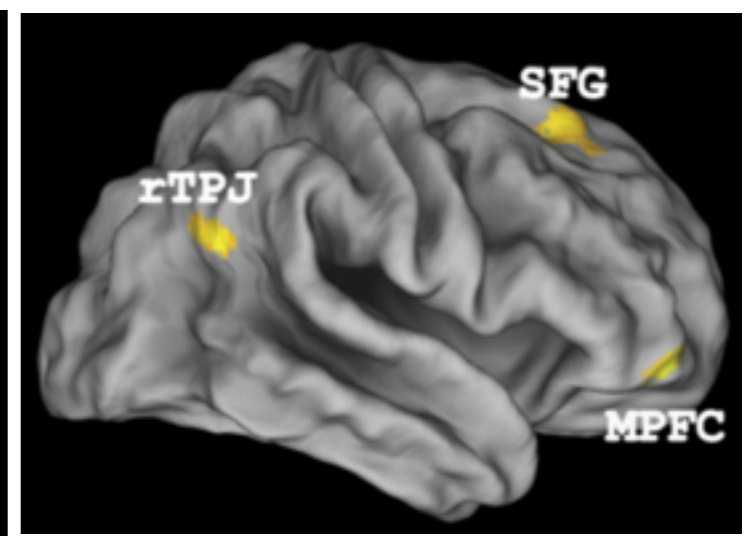
Non-painful



Painful



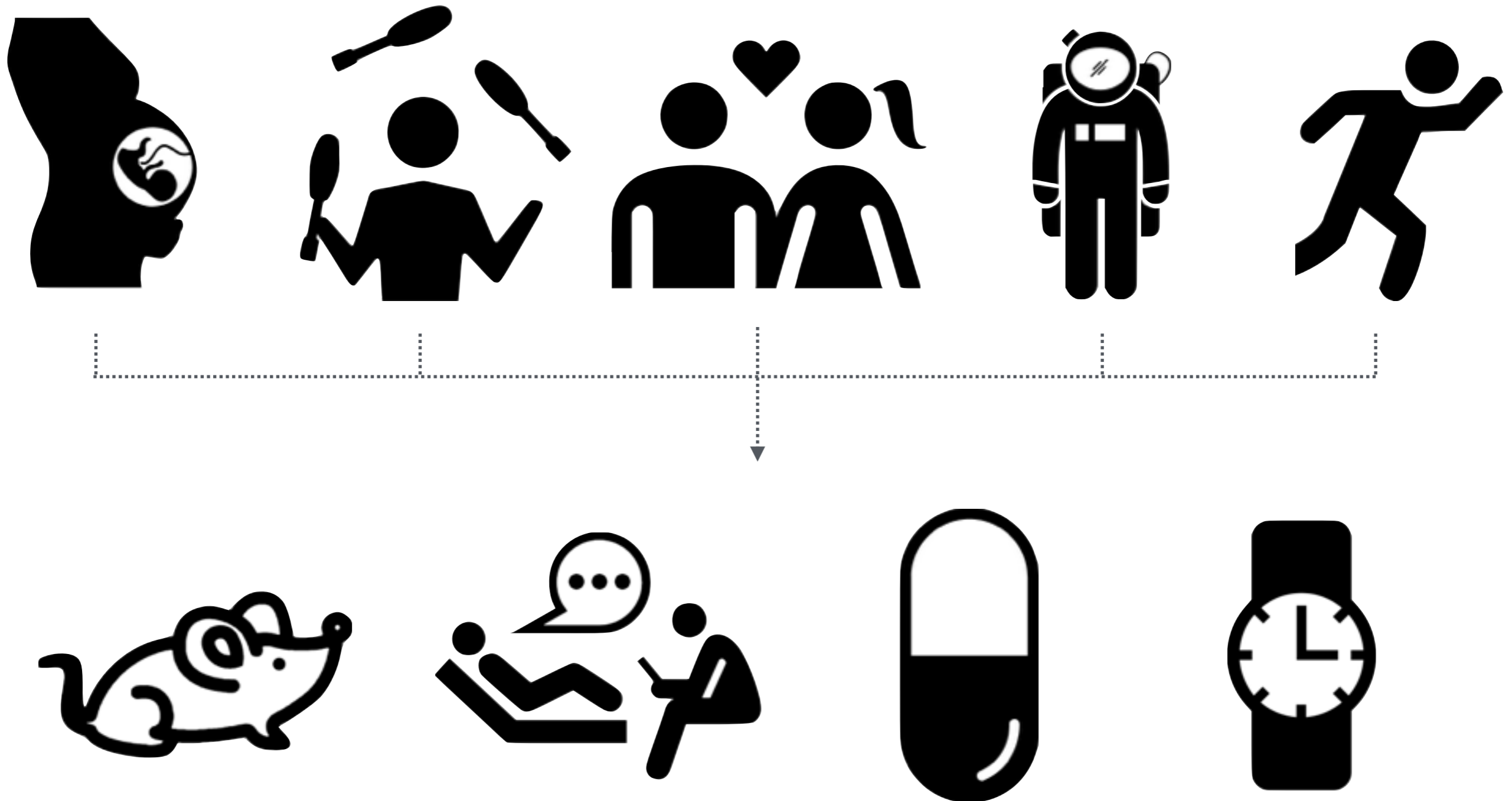
Non-painful



Love can be measured !?



# Deconstructing the **framework** of scientific papers !



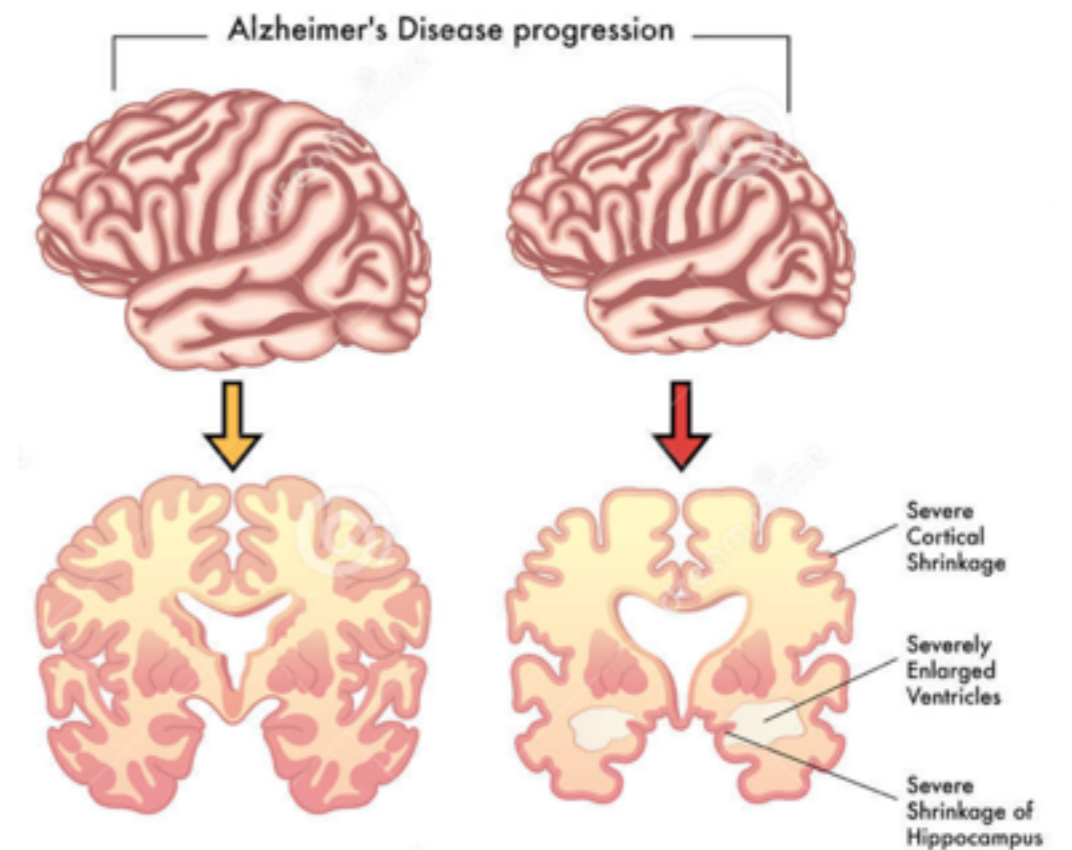
Experimental, intervention, medication and time effect in **single group**.....

[Pair T test]

Example 2:

Gray matter volume atrophy in patient with Alzheimer's disease !?

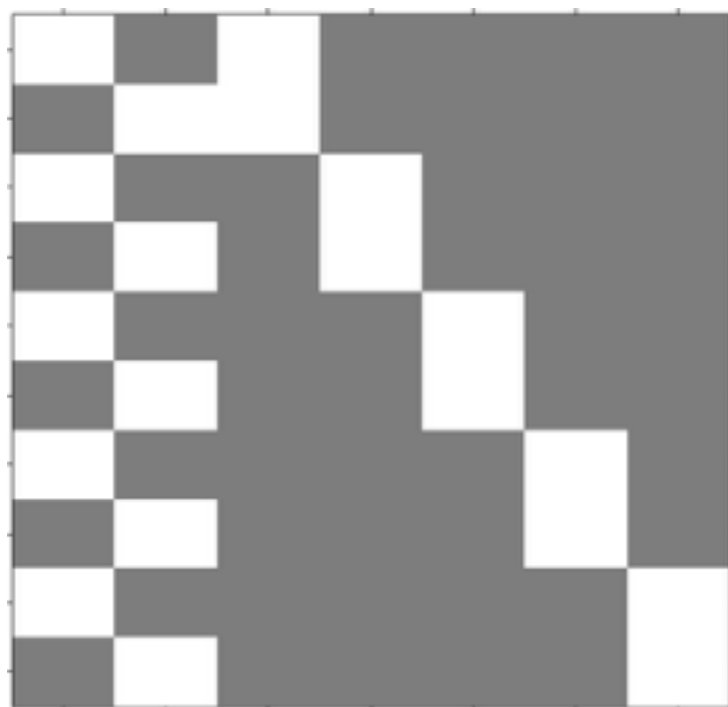
---



# Longitudinal GMV changes in patients with Alzheimer's Disease

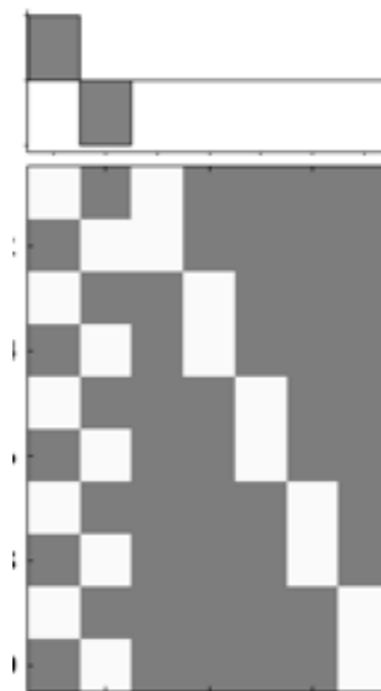
“Is there significantly **lower gray matter volume** in the follow-up scan than in the baseline scan of the patient with Alzheimer disease?”

$$Y = \beta_1(\text{baseline}) + \beta_2(\text{follow-up}) + \beta_3(\text{within-subject 1 effect}) + \dots + \beta_n(\text{within-subject } n \text{ effect}) + \varepsilon$$

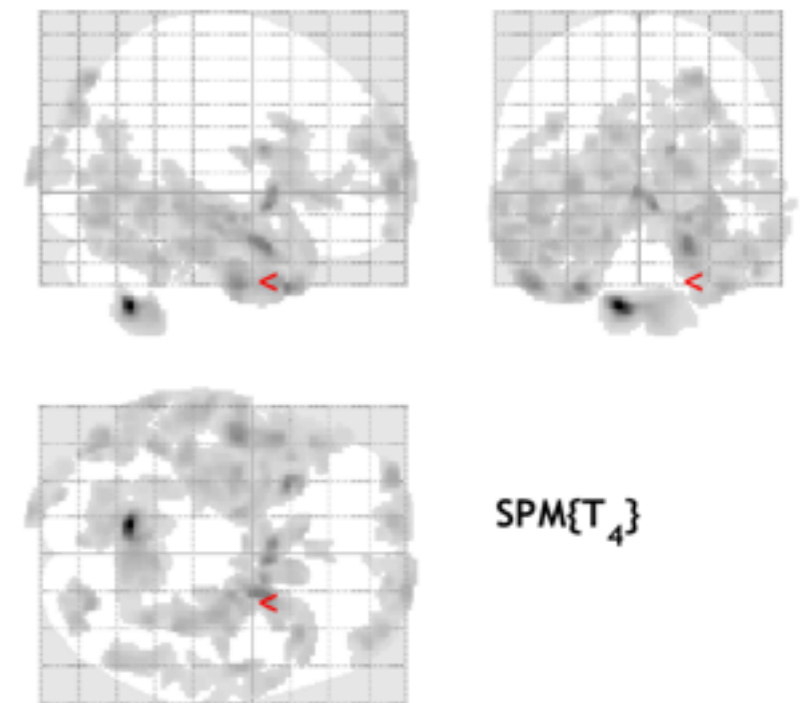


1st 2nd Within subject effect

Model construction

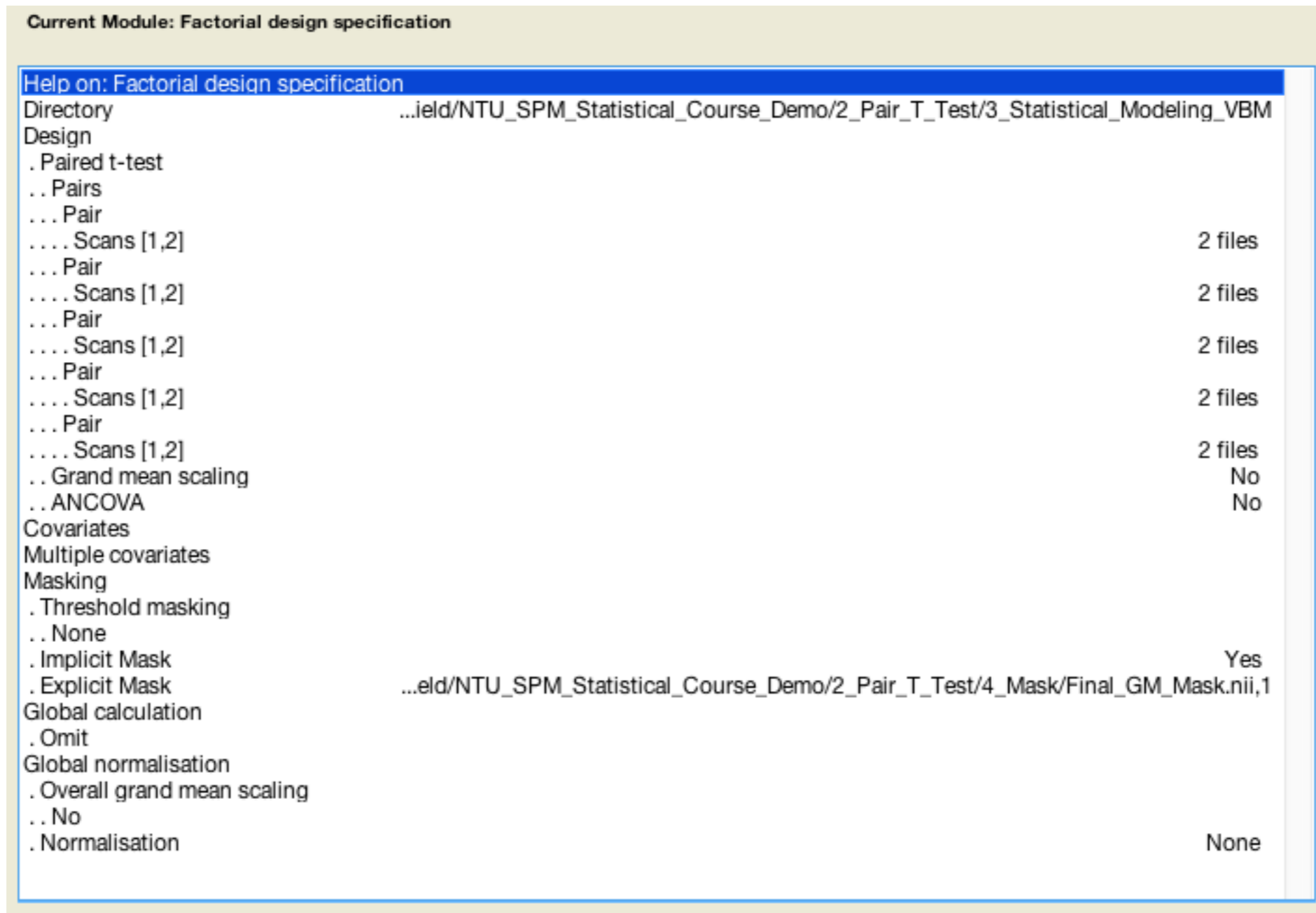


Statistical inference



Result visualization

# Pair T-test (Model Construction)

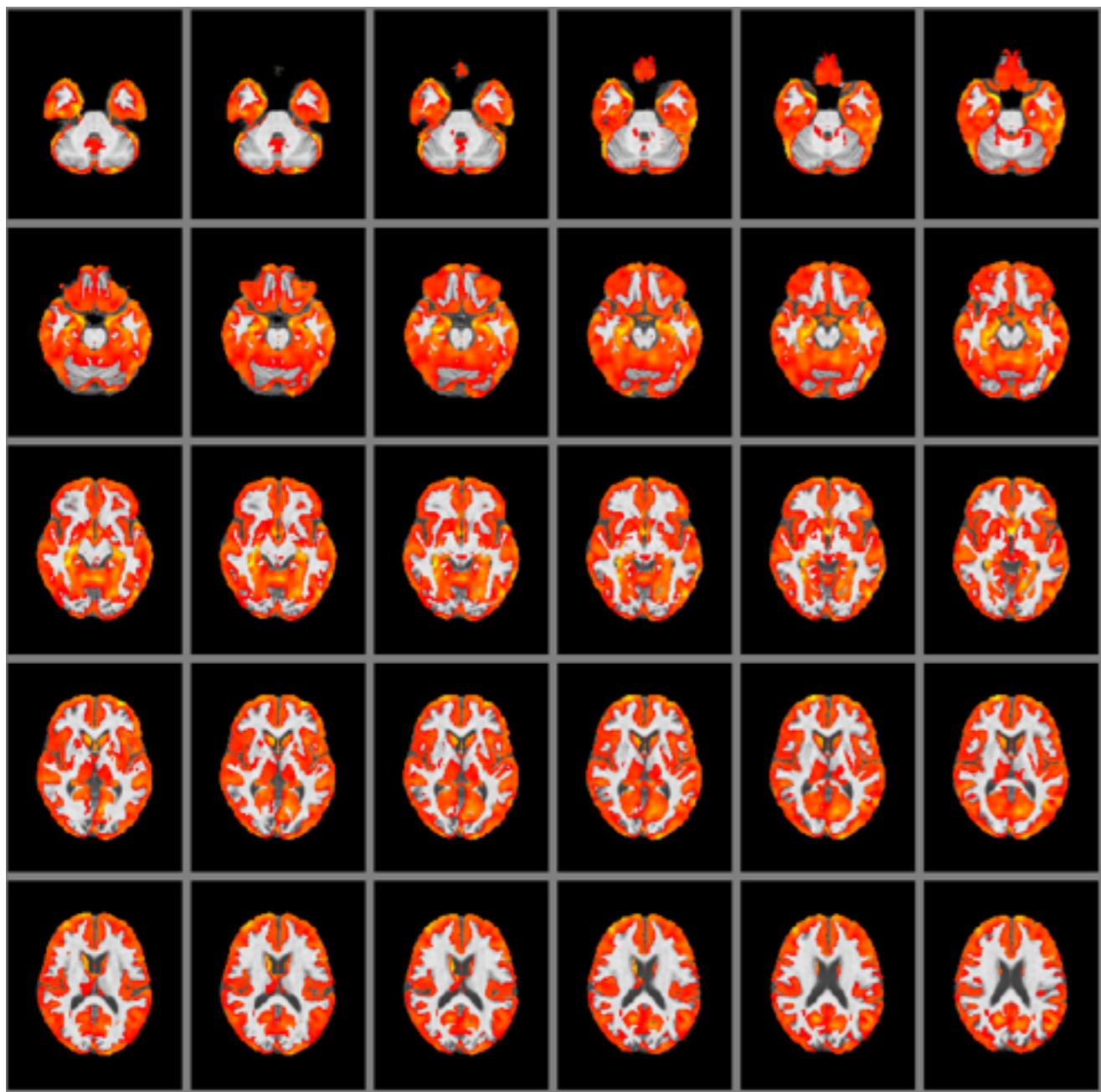


**Directory:** The output directory of your statistical model

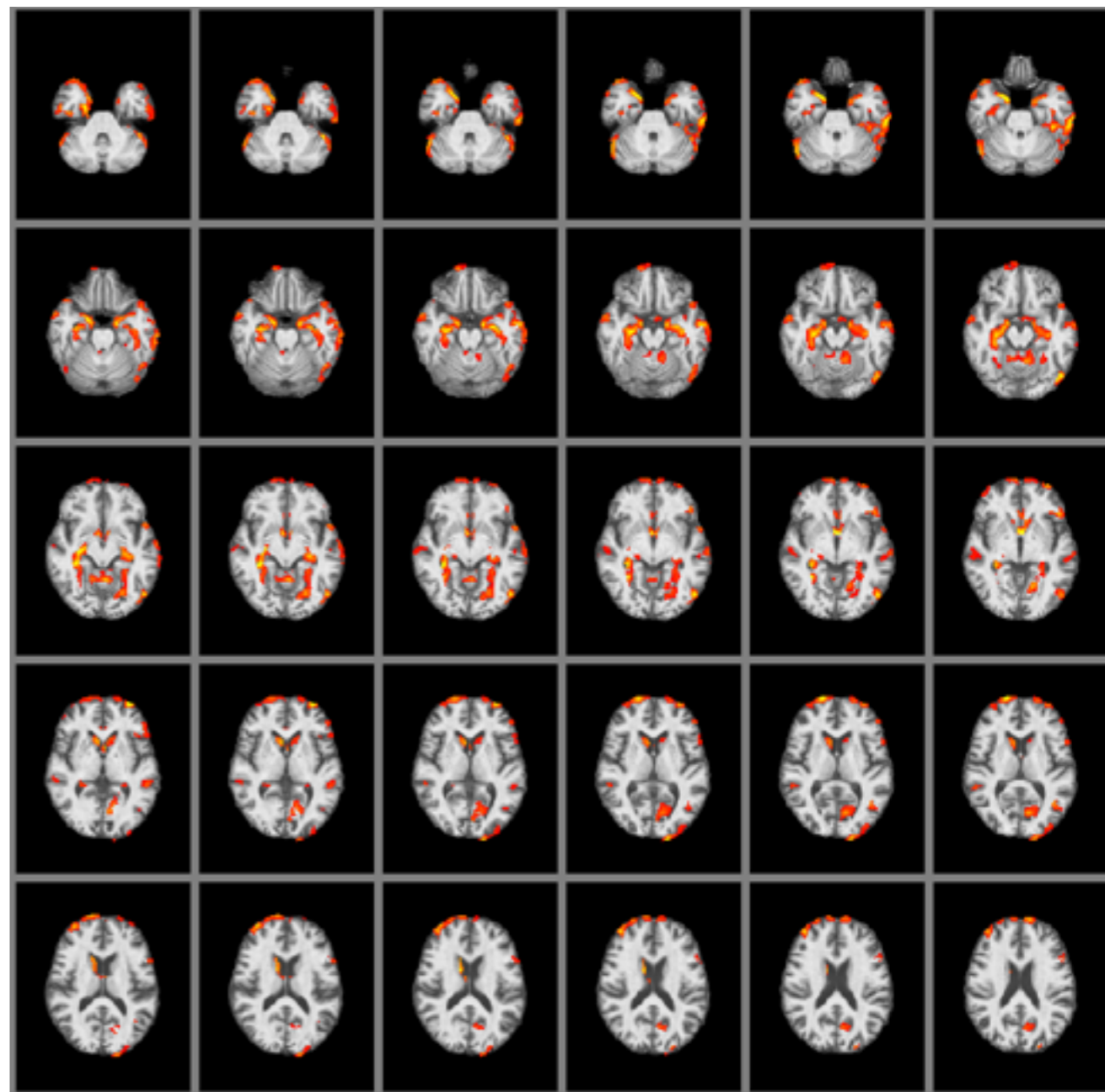
**Design:** The statistical model you want to use (**Pair T-test**)

**Masking:** The region you want to do statistical inference

# Statistical **result** of our question !



un-thresholded map

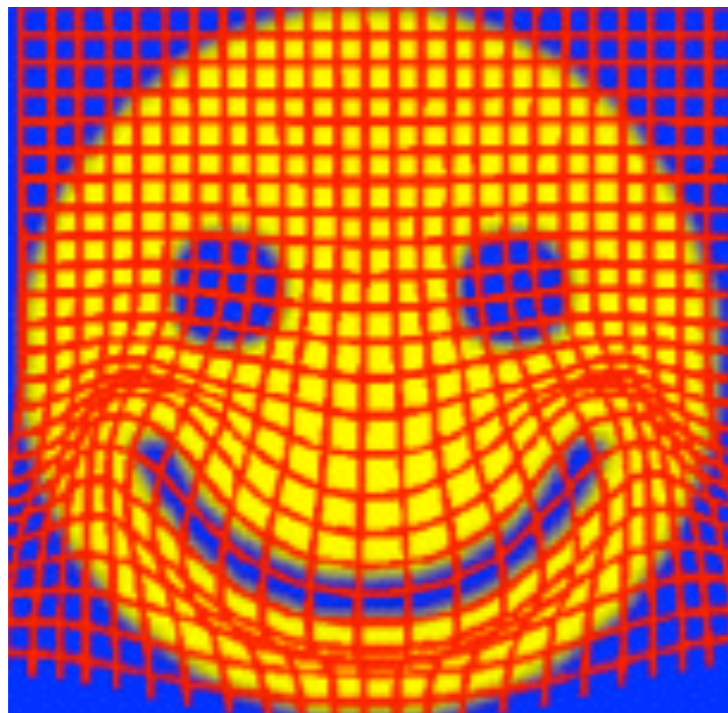
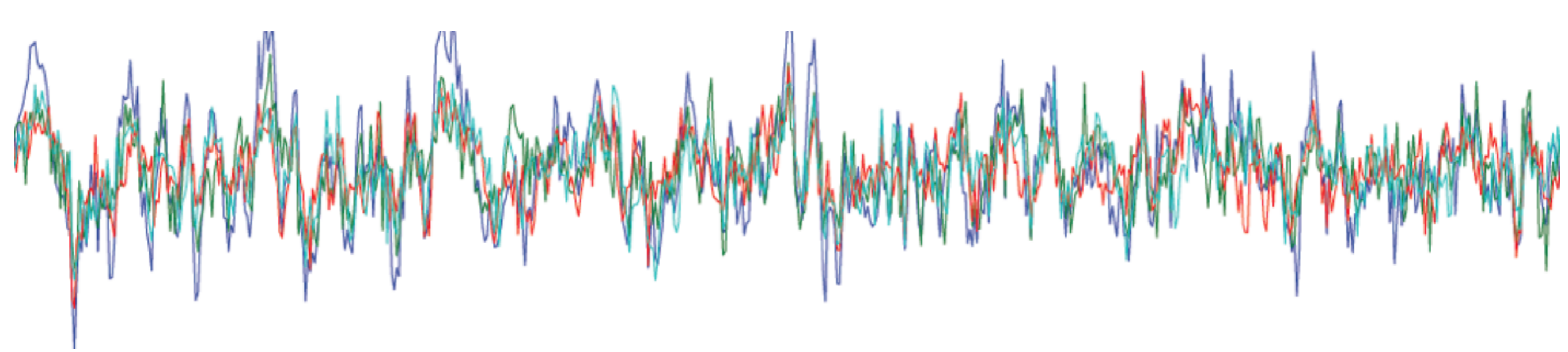


thresholded map

# TL;DR

Number of factor levels	Number of covariates	Statistical model
1	0	One-sample T-test
1	1	Single regression
1	> 1	Multiple regression
2	0	Two-sample T-test
> 2	0	ANOVA
> 2	> 0	ANCOVA (full factorial)

Special case : Pair-T test (before-after effect in single group)



Thanks for your attention !!

 [dargonchow1@gmail.com](mailto:dargonchow1@gmail.com)